# Structure and Properties of Oriented Poly(ethylene Terephthalate) Films

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#### Synopsis

A study was made of the structural and property changes that occur when poly(ethylene terephthalate) films are oriented, crystallized, and thermally relaxed. X-ray diffraction, infrared, density, and stress-strain measurements were used to develop information on the amount and direction of orientation of both the crystalline and amorphous regions of these films. Three structural factors influence resultant film properties: (1) the kind and perfection of crystallite orientation, (2) the amount and direction of the *trans-gauche* isomerization in the amorphous regions, and (3) the amount of crystallinity. Interactions of these factors result in substantially different film properties and relaxation behavior. Of special significance is the influence of "taut" extended amorphous regions produced by orientation which generate useful structure-property information.

The properties of polymeric fibers and films depend to a large extent on the orientation produced during processing. Oriented semicrystalline polymers, such as poly(ethylene terephthalate) are believed to consist of crystalline and amorphous regions distributed in various ways depending on the extent and kind of processing techniques used. It is convenient to depict these oriented polymer structures in accordance with a modified fringed-micelle model, having a range of degrees of order in both the crystalline and amorphous regions.

As discussed earlier,<sup>1</sup> a real need exists for the direct determination of the distributions of both the crystalline and amorphous regions to establish the mechanisms taking place during orientation. The requirements to accomplish this are: (1) a systematic geometrical reference system for the several types of orientation possible and (2) experimental methods for the independent determination of the distributions of each kind of structural region. The first of these requirements is satisfied by the orientation definitions that have been given. The second requirement is partially accomplished by single-crystal x-ray techniques which provide the means to measure the orientation distributions of the crystalline regions, and also by recent infrared studies which characterize the amorphous regions of the polymer. Assumed distribution functions that have appeared in the literature do not satisfactorily explain the observed orientation phenomena, nor take into account the different types of distributions found to exist in polymeric systems.

Schmidt<sup>2</sup> and others<sup>3</sup> using polarized infrared techniques have shown the importance of a more detailed division of structure, in addition to the crystalline-amorphous division for poly (ethylene terephthalate) films. This division is based on the molecular conformations of the ethylene glycol linkage which in poly (ethylene terephthalate) may exist in either of two rotational isomeric forms (*trans* or *gauche*). The *trans* isomer is the extended form relative to the *gauche* and occurs in both the crystalline and amorphous regions of the polymer; the *gauche* isomer, however, occurs only in the amorphous regions. A film with a given amount of crystallinity may have varying amounts of *trans* isomer; likewise a film with a given amount of *trans* isomer may have varying amounts of crystallinity.

With these techniques in hand, it now appears that many of the experimental problems in measuring the complete orientation distributions of the polymer structural elements have been solved, and it is the intent of this paper to show how the results of several of these experimental techniques, i.e., x-ray, infrared, stress-strain results, etc., when viewed together, provide a comprehensive view of the structure of oriented poly-(ethylene terephthalate) films. It is also an objective of this paper to demonstrate the contribution of the amorphous regions to an understanding of structural changes and how they influence the mechanical and thermal properties of oriented crystalline polymeric films.

To present this information in an orderly fashion, we will describe first the methods used to measure specific structural parameters and then define how these parameters change as a film is taken through several orientation processes. Interpretations are given which describe the structural changes that influence specific film properties.

The structural parameters studied were (1) the crystallite orientation distributions, (2) the crystallite length, (3) the long-period spacing and the amorphous length as given by low-angle x-ray diffraction, and (4) changes in the absorbance and direction of selected infrared bands (*trans-gauche* isomerism).

Since the start of the work reported here, an excellent paper has appeared<sup>4</sup> which describes the molecular structure and some of the mechanical properties of poly(ethylene terephthalate) fibers. Significant structural changes, however, occur from biaxial stretching not seen by the uniaxial stretch of a film or fiber.

#### **Terminology and Experimental Techniques**

Previously,<sup>1</sup> orientation definitions (e.g., uniplanar, uniplanar-axial) were given to describe the kinds of structure produced in oriented films or fibers. An important attribute of these definitions is that they apply to the system as a whole, even though various kinds of experimental manipulations and orientation measurements may be required to generate the complete orientation figure.

The initially unoriented poly(ethylene terephthalate) films studied were stretched and analyzed in the sequence: (a) longitudinally stretched

(M.D.), (b) then transversely (T.D.) stretched, and (c) finally poststretched (M.D. again).

### **Crystallite Orientation Distributions**

In polymer structures, orientation is not perfect, and distributions of directions of crystal planes or axes will be observed. It is also possible for several orientation types to coexist within the same sample. Substantial information can be generated from the crystallite orientation distributions measured by the single crystal orienter (SCO) technique. All x-ray measurements utilized  $CuK\alpha$  radiation at 50 kv. and 16 ma. As reported earlier, the crystallite orientation distributions are in fact surfaces generated from a composite of individual distribution measurements obtained from These surfaces provide an excellent qualitative undersample rotations. standing of the nature of the crystallite orientation but, as has been shown,<sup>5</sup> are difficult to describe quantitatively. Our attempts to achieve a mathematical expression to fit the many kinds of orientation surfaces generated by the several process steps, involved functions with as many as seven parameters. With the additional problem of describing a large number of samples, the effort was abandoned for the following reasons: (1) the surfaces we did fit with equations added nothing to our understanding of the processes that occur; (2) even though the functions worked for a particular sample, the coefficients had no significant physical meaning; (3) it is possible to calculate an orientation parameter by using only the distribution curve at maximum orientation which correlates with other structural A simple and useful technique for describing the curves was features. suggested by Hoerl<sup>6</sup> and was used to define the average orientation of either a crystallite plane or axis. Hermans et al.<sup>7</sup> and Wilchinsky<sup>5</sup> have used a similar approach but have incorporated into their calculations the average trigonometric functions to define an orientation factor. We feel that the method used here is just as useful and can be calculated somewhat more quickly. The numbers we generate are representative of the average position of a major crystallite plane, (100) relative to the film surface designated  $\sigma_{p,p}$  and the c axis of the crystallite relative to the direction of stretching or rolling  $\sigma_{a,a}$ . Values obtained are in degrees, where 0° denotes perfect parallelism and 45° denotes complete randomization of the operator to reference system. The method is described in the Appendix.

#### **Infrared Studies**

Infrared studies have also yielded information concerning the orientation of poly(ethylene terephthalate). Parameters characteristic of the molecular axial  $(\Delta_a)$  and uniplanar  $(\Delta_a)$  orientations were defined,<sup>2</sup> where

$$\Delta_a = A_x / A_y \ (875 \text{ cm.}^{-1})$$

and

$$\Delta_p = A_z / A_y \ (875 \text{ cm.}^{-1})$$

 $A_z$ ,  $A_y$ , and  $A_z$  are the absorption intensities of the 875 cm.<sup>-1</sup> infrared band along the mutually perpendicular directions, machine, transverse, and normal to the film surface.

Initially, we had expected that only the infrared technique would be needed, since the x-ray  $\sigma$  and infrared  $\Delta$  values seemed to correlate in many of the samples investigated. However, we found that this was not a reliable correlation, because the amorphous orientation can change substantially without influencing to any great extent the crystallite orientation. Samples subjected to small amounts of stress or strain relaxation due to post heat treatments will show a greater rearrangement of direction of chain segments in the amorphous regions than in changes in the directions of the crystallites. Therefore, independent measurements of both the crystalline and amorphous structure are required.

#### **Measurement of Crystallite Length**

In poly(ethylene terephthalate), the broadening of the ( $\overline{105}$ ) diffraction peak, observed in this study at  $2\theta = 42.8^{\circ}$ , is used to measure the crystallite length. The ( $\overline{105}$ ) makes an angle of 88.0° with the *c* axis and hence can, for the purposes of crystallite length measurement, be considered normal to it. For the lattice parameters as determined by Daubeny et al.<sup>8</sup>  $2\theta$  for thus plane is 46.0°. Evidence for the identity of the ( $\overline{105}$ ) is as follows: (1) structure factor calculations of all the possible planes in the  $2\theta$  region from  $41.8^{\circ}$  to  $47.0^{\circ}$  indicate that the ( $\overline{105}$ ) is the strongest reflecting plane, (2) other planes are not likely to be in position to diffract from the orientation produced by stretching, and (3) none of the other planes have a calculated  $2\theta$  at  $46.0^{\circ}$ . The discrepancy between the observed and calculated  $2\theta$ has not been resolved but may be due to slight differences in lattice parameters from those reported.

The theory and assumptions used for crystallite size measurements by line broadening are adequately covered elsewhere.<sup>9</sup> Average crystallite lengths were calculated by using Warren's correction for the Scherrer line broadening equation. The value for instrumental broadening for our x-ray instrument was determined by using finely powdered zinc oxide scanned at  $0.2^{\circ}/\text{min}$ . from below a  $2\theta$  angle of  $30.0^{\circ}$  to greater than  $47.0^{\circ}$ with nickel-filtered CuK $\alpha$  radiation. The broadening of the ZnO reference diffraction peaks was averaged, and a value of  $0.678^{\circ}$  for the instrumental broadening correction was obtained.

The errors in the crystallite size measurements are of the order of  $\pm 3$  A. Increased precision of the results can be obtained by refinements in technique such as scanning slower, but the assumptions used in the linebroadening equations make the virtue of increased precision doubtful. Primary interest was not in the absolute values of crystallite size but in how size changed with orientation.

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#### **Intercrystalline Spacing**

In addition to the directional arrangement and size of the crystalline regions, the influence of the intercrystalline spacing helps explain some of the properties observed in poly(ethylene terephthalate) films. The orientation distribution of the crystallites does allow one to infer to some extent what is occurring in the amorphous regions. Low-angle x-ray techniques, however, not only provide a measure of intercrystalline spacing but also help develop further insight into the amorphous character of poly(ethylene terephthalate) films.

Statton<sup>10</sup> and others<sup>11,12</sup> expanding the work of Hess and Keissig<sup>13</sup> have formulated structural interpretations to explain low-angle x-ray diffractions in fibers. These interpretations have been used to explain some of the low-angle diffraction characteristics of the films studied.

The low-angle diffraction is thought to originate from a periodic spacing of the crystallites. A line lattice is formed by the crystallites over a short range, and the long-period spacing can be calculated by using the Bragg equation. The long period presumably is an average spacing of the crystallite plus the amorphous region, and the calculated values given are average values characteristic of the center-to-center spacing of the somewhat diffuse spots which occur.

The long-period spacings of poly(ethylene terephthalate) films were measured by using a sample thickness of 0.020 in., CuK $\alpha$  radiation at 50 kv. and 16 ma. with a sample-to-film distance of 17 cm. in a vacuum camera. Three types of exposures are commonly made, designated "edge" (x-ray beam normal to the M.D. axis, i.e., along the T.D. axis), "end" (x-ray beam parallel to the M.D. axis, i.e., normal to the T.D. axis), and



Fig. 1. Low-angle x-ray diffractions for one-way stretched films.

"thru" (x-ray beam normal to the film surface). These are identified in Figure 1. The values from the edge exposures were used for the longperiod measurements and for the calculations of a so-called amorphous length. The amorphous length is calculated by subtracting the average crystallite length obtained from line broadening from the long-period spacing.

## **Stress-Strain Character of Film Samples**

The tensile properties, modulus, strength, elongation, and others are useful in determining the results of orientation introduced in films or fibers. Typical stress-strain curves for one-way, two-way, and post-stretched films are as shown in Figure 2. Experimental procedures for the measurements of the tensile properties of poly(ethylene terephthalate) films have been described by Amborski and Flierl.<sup>14</sup> The curve shapes obtained during tensile testing in several directions reflect orientation differences quite dramatically.

Tensile modulus at 1% elongation is a measure of the stiffness of the film and tensile break strength is indicative of the perfection of orientation. Elongation can be considered as a measure of the mobility of the chains



Fig. 2. Stress vs. strain for films: (I) one-way stretched, not heat-set; (II) two-way stretched, balanced heat-set; (III) post-stretched, heat-set.

	Amor- phous trans, %	13 14 20 24	38 38 48	Amor- phous trans, $7_0$	11 25 26
	Crystalline trans, %	0 14 17	25 27 30	Crystal- line <i>trans</i> ,	84 84 84 84 84 84
	Total trans, %	13 21 41	56 55 78	Total trans, %	- 59 73 74
	morphous length, A.	853	50 50 48	Amor- phous length, A.	64 61 55 56
ure)	ystallite A ength, A.	55 24   58 51 4	60 63 65	Heat-Set Crystal- lite length, A.	48 52 58 64
I Ims (Structu	ong Tiod, 1 A.	102	2 2 2 2 2	I tructure), H Long period, A.	119 113 120 120 120
TABLE tretched Fil	<u>ъ</u> 8 г	1 2 3 5 5		TABLE I ed Films (S $\Delta_p$	1.45 1.22 1.38 1.39 1.85
One-Way Si	$\Delta_p$	1.00 1.05 1.22 1.39	1.70 1.86	∕ay Stretch ∆a	).90 [.74 0.99 [.97
•	$\Delta_{a}$	1.00 1.41 1.74 1.97	2.21 2.47 2.68	Two-W	~ 6 ~ 6 6
	¢(p,p), °	45.0 37.1 30.9 25.9	21.4 18.1 17.4	ه <sup>(4,4</sup> ) م	30. 14. 11.
	(a.a), <sup>0</sup>	45.0 27.7 21.3 18.0	14.5 11.8 12.2	ط (و, a)	47.3 21.3 42.3 18.0 36.1
	Stretch ratio $\sigma$	As cast 3.0 3.5	4.0 5.0 5.0	Stretch ratio	2.5×2.5 3.0 3.0×3.0 3.5×3.5 3.5×3.5

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	Amor- phous trans, %	35 40 46		ion, %	T.D.	497	490	400	474		402
	Crystal- line trans, %	43 43 43 43		Elongat	M.D.	214	92	68	48		10
	Total trans, %	67 88 88			T.D.	7,000	5,870	5,660	7,800	7,563	8,138
	Amor- phous length, A.	71 75 85		$F_{5}$ , psi <sup>a</sup>	(.D.	000	000	300	500	350	200
ture)	Crystal- lite length, A.	60 57 56	perties)		M	9,	16,	19,	24,	33,	40.
LE III Films (Strue	$\begin{array}{c c} TABLE III \\ \text{ost-Stretched Films (Struct)} \\ \hline A_p \\ \Delta_p \\ \Delta_p \\ A. \\ A. \\ A. \\ 1.72 \\ 1.72 \\ 1.8 \\ 1.8 \\ 1.65 \\ 141 \end{array}$	LE IV ed Film (Pro	ength, psi	T.D.	6,470	6,540	7,090	6,520	7,410	7,290	
TAB Post-Stretched		1.72 1.78 1.65	TAB TAB	Tensile str	M.D.	16,900	26,000	31,800	40,800	47,318	57,744
Π	$\Delta_a$	1.23 1.30 1.46	S		T.D.	28,000	99,000	65,000	53,000	03,000	31,000
σ(a, a), σ(p, p), σ 37.5 16.0 36.5 15.9 26.0 15.0	16.0 15.9 16.2		odulus, psi		3	0	0	0	3(	3	
	G(a,a), <sup>0</sup>	37.5 36.5 36.2		W	M.D.	460,000	883,000	1,018,000	1,276,00	1,546,000	1,772,000
	Stretch ratio	1.30 1.45 1.68		Stretch	ratio	2.0	3.0	3.5	4.0	4.5	5 0

<sup>a</sup>  $F_b = \text{tensile stress at } 5\%$  elongation.

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	Modi	ulus, psi	Tensile st	rength, psi	F 5,	psi	Elongati	ion, %
tretch ratio	M.D.	T.D.	M.D.	T.D.	M.D.	T.D.	M.D.	T.D.
$2.5 \times 2.5$	624,000	700,000	19,500	23,200	13,500	14,000	128	140
$3.0 \times 3.0$	655,000	641,000	26,500	22,400	14,600	14,400	114	135
$1.5 \times 3.5$	759,000	674,000	30,500	24,300	15,500	14,700	78	100
Utrat ch	Modulue	s, psi	Tensile str	ength, psi	$F_{5}$	psi	Elongat	tion, %
ratio	M.D.	T.D.	M.D.	T.D.	M.D.	T.D.	M.D.	T.D
1.30	921,000	564,000	37,000	21,000	20,100	12,000	40	150
1.45	994,000	463,000	38,200	17,000	26,600	10,800	52	250
1 60	1 050 000	-00			001 100	000 11	t (	100

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under stress while the  $F_5$  (the force required to elongate the sample 5%) is a measure of the tautness of the polymer chains. Each of these characteristics provides a qualitative idea of what the sample was structurally, prior to testing.

On the basis of the kinds of measurements discussed, made on many samples, we shall describe now what we believe to occur during the stretching of poly(ethylene terephthalate) films. Our conclusions are based on the combinations of the changes in the structural parameters we have been able to measure. In this discussion we hope to convey to the reader the significance of the interaction between crystallite orientation and of an extended "taut" amorphous structure on the useful properties of a polymetic film.

	One-V	Way Stretched	Films (Struct	ure)	
Stretch ratio	$\Delta_a$	$\Delta_p$	Total trans, %	Amorphous trans, %	Crystalline trans, %
		Not Hea	ıt-Set		
4.0	2.21	1.70	56	31	25
4.5	2.43	1.77	65	38	27
5.0	2.68	1.86	78	47	31
5.5	2.96	1.91	89	55	34
		Heat-S	Set		
4.0	1.78	1.50	67	19	48
4.5	1.98	1.55	74	26	48
5.0	1.90	1.65	77	29	48
5.5	2.36	1.83	82	34	48

TABLE VII

TABLE VIII Two-Way Stretched Films (Structure)

Stretch ratio	$\Delta_a$	$\Delta_p$	Total trans, %	Amorphous trans, %	Crystalline trans, %
		Not Heat-	Set		
$2.0 \times 3.5$	0.828	1.60	41	24	17
$3.0 \times 2.5$	1.02	1.60	42	24	17
$3.0 \times 3.0$	0.973	1.76	52	35	17
$3.5 \times 3.0$	1.14	1.69	51	35	17
$3.5 \times 3.5$	1.02	1.63	51	35	17
		Heat-Set	;		
$2.0 \times 3.5$	0.712	1.84	63	16	47
$3.0 \times 2.5$	1.15	1.92	63	15	48
$3.0 \times 3.0$	0.991	1.88	73	25	48
$3.5 \times 3.0$	1.12	1.82	77	29	48
$3.5 \times 3.5$	1.13	1.85	74	26	48

Stretch			Total trans,	Crystalline trans,	Amorphous trans,
ratio	$\Delta_a$	$\Delta_p$	%	%	%
		Not Heat-I	Relaxed		
3.5	1.97	1.39	41	17	24
4.0	2.21	1.70	56	25	31
4.5	2.47	1.77	65	27	38
5.0	2.68	1.86	78	31	47
5.5	2.96	1.91	89	34	55
		Heat-Re	laxed		
	1.41	1.39	28	17	11
	1.62	1.66	38	<b>25</b>	13
	1.84	1.68	48	27	21
	2.22	1.58	58	31	27
	2.10	1.60	61	34	27

TABLE IX One-Way Stretched Films (Structure)

TABLE X Strain Relaxation of One-Way, Two-Way, and Post-Stretched Films

Sample	M.D. relaxa- tion, %	Density g./cc.	MD F₅, psi	MD elonga- tion, %	Long period, A.	Crystal- line length, A.	Amor- phous length, A.
Sample 1, post- stretched	0.0 0.6 4.4	1.3799 1.3809 1.3814	23,200 21,548 17,855	26.4 23.5 41.8	132	64	68
	7.6 10.8	1.3850 1.3878	16 ,582 15 ,735	52.0 42.5	120	64	56
0 1 0	14.8	1.3942	15,029	46.9	115	63	52 59
way stretched	$\begin{array}{c} 0.0\\ 3.2\\ 10.5\end{array}$	1.3839 1.3843 1.3924	32,761 22,718 19,100	24 31 36	115	57 61	58 53
	15.5	1.4011	529, 16	45	110	62	58
Sample 3, two- way stretched, $3.5 \times 3.5$	0.0 10.7	1.3932 1.3999	15, <b>46</b> 8 14,750	80.8 99.7	120 120	58 57	62 63

The structural changes that take place in an initially amorphous unoriented film as it is taken through several stretching procedures are described below. Experimental results are presented in Tables I-X. The values given are average results of duplicate samples.

## **One-Way Stretched Films**

Quenched amorphous poly(ethylene terephthalate) film with  $\overline{M}_n \cong 15,000$  is a mixture of molecular chains of varying lengths having no unique directivity. In this state the chains are most likely coiled, folded, or both, and extremely tangled. The orientation of this structure is called random.

When this amorphous film is M.D. stretched, the molecular chains become partially aligned along the stretch direction and some crystallization occurs. The crystallites formed, in general, have their c axes, i.e., the long axis of the poly(ethylene terephthalate) crystallite, parallel to the direction of stretch, and some fraction of the (100) crystallite planes are aligned parallel to the surface of the film. As the amount of stretch is increased, the alignment of the c axes relative to the direction of stretch is improved, as are also the alignment of the (100) planes relative to the film surface (Table I). The resulting structure is classified as uniplanar-axial orienta-Since the molecular chains were most likely initially tangled and tion. randomly oriented, many chain segments probably remain entangled after the M.D. stretch. In fact, a fibrillar type structure is presumed to have been formed. Under the stretching conditions we used here, at stretch ratios greater than about  $3.5 \times (3.5 \text{ times or } 250\% \text{ of the initial length})$  the chains are believed to be so strained that there are many "taut" oriented amorphous regions between the crystallites. In other words, many chain segments are extended, and rather limited, by entanglements with other taut chains or crystallites in how far they can be further stretched. As a result, the slope of the initial portion of the stress-strain curve is steep, and  $F_{5}$  values above 20,000 psi are produced (Table IV). The transverse direction properties remain essentially unchanged. X-ray measurements tell us that the distance between crystallite centers is about 112-114 A. for one-way stretched films, and that the distance between crystallite "edges" (the amorphous length) decreases with increased orientation (Table I). The crystallite length produced is dependent upon the extent to which the film is stretched, i.e., the higher the stretch ratio, the longer the crystallite length, since the crystalline regions can grow more easily as the alignment of chains in this direction is improved (Table I).

Infrared studies show the cast amorphous poly(ethylene terephthalate) films to be randomly oriented and to contain a fixed amount of trans-gauche structure. In these films, there is approximately 13% trans structure and 87% gauche structure. Since the trans structure is an extended form, this indicates that the majority of molecules are in a relaxed, unextended state. When the cast film is M.D. stretched and the molecules become aligned along the stretch direction, the individual chain segments become extended; that is, some gauche poly(ethylene terephthalate) is converted into trans poly(ethylene terephthalate) (Table I). The trans isomer is the only one that exists in the crystalline regions, and some crystallization will occur as the trans isomers are brought into proximity while being aligned along the stretch axis (Table I). For stretch ratios below  $3.5 \times$ , there is only a small amount of preferred orientation of the phenyl rings relative to the plane of the films. As the stretch ratio approaches  $3.5 \times$ , a significant fraction of the chain segments have been aligned and placed in the taut extended trans configuration; further stretching puts additional stress on the trans segments and twists them into a position which will facilitate greater crystalline growth. At this point, the planes of the phenyl rings are approximately parallel to the plane of the film (Table I). As stretching is continued beyond  $3.5\times$ , the *trans* content of the film increases, the *gauche* content decreases, the amount of amorphous *trans* increasing at a rate more rapid than the amount of *trans* from crystallization (Table I). The alignment of the molecular chains to the stretch direction and the alignment of phenyl rings to the plane of the film also increase (Table I). Since the *trans* isomer of poly(ethylene terephthalate) is extended relative to the *gauche* isomer, the amount of *trans* structure at a given level of crystallinity is a measure of the "tautness" of the amorphous regions of the polymer and it is directly related to the modulus, strength, elongation, and  $F_5$  values of the film (Table IV).

# **Two-Way Stretching**

Subsequent stretching of the one-way M.D. stretched film in the transverse direction causes the chain segments in the amorphous regions and the crystallites to be shifted from the machine direction toward the transverse direction, the amount of this movement being dependent upon stretch ratio, temperature, and other process conditions. From this treatment, some of the crystallite c axes move from the M.D. toward the T.D., the amount of this movement measured by the crystallite orientation distribution parameter  $\sigma_{(a,a)}$ . In addition, the (100) planes of the crystallites are forced into better parellelism with the surface of the film, as measured by the crystallite orientation parameter  $\sigma_{(p,p)}$  (Table II). Values for the oneway stretched film are included in Table II for comparison. It is believed that during the second direction stretch some chain disentanglements occur, since the long period (the distance between crystallite centers in the M.D.) increases to 119-120 A. (Table II). The crystallite length, however, increases slightly over that produced by the first direction stretch and, therefore, the average amorphous length is essentially unchanged. The structural changes that take place during the second direction stretch are primarily associated with the reapportionment of the structure that has been produced by the first direction stretch. The amorphous regions of this film are not as highly strained in either the M.D. or T.D. and as a consequence the initial part of the force elongation tensile curves have a lower slope and resultant lowered modulus and  $F_5$  (Table V) than one-way stretched films. The shifting of some of the orientation from M.D. toward the T.D. has now generated comparable properties in the two directions. At balance the orientation is uniplanar. During the second direction stretch a slight increase in the amorphous trans content occurs (compare Tables I and VIII). Additional changes occur due to crystallinity.

#### Crystallization

The production of dimensionally stable films requires that the structure introduced by these orientation steps be immobilized through crystallization. This process has become known as heat setting. Only the *trans* isomers are capable of crystallizing. Crystallization may be induced in either of two ways: by polymer stretching or by heat setting at temperatures substantially higher than the glass transition: As noted before, gauche poly(ethylene terephthalate) is transformed into trans poly(ethylene terephthalate) during the stretching process (Tables I and VIII). Here many trans isomers are brought into proximity of one another; hence crystallization occurs. Crystallization induced by the heat-setting process may come about by either the movement of amorphous trans molecules into the necessary proximity or by the thermal isomerization of gauche near neighbors with a subsequent crystallization of the newly formed trans material. The latter explanation is more plausible, since the amorphous trans content changes only about one-third that of the trans crystalline change during the crystallization of two-way stretched films (Table VIII).

Tension on the film samples during crystallization plays an important role in the development of structure. Generally, if a one-way stretched film is heat-set under tension to try to maintain the orientation produced by stretching, the total *trans* content of the film increases (Table VII) as the crystallinity increases. The larger the initial *trans* content, the smaller will be the subsequent increase, since the remaining *gauche* content that can be converted to *trans* will be small. The degree of molecular orientation of this film, however, will decrease (Table VII). Evidently the orientation stresses are so great that they cannot be completely restrained by tension on the film during crystallization so that stress decay, localized melting, and recrystallization occur. The parameters characteristic of both the molecular axial and uniplanar orientation decrease in value. We will refer to this process as structural relaxation as contrasted to strain relaxation.

During the restrained crystallization of a two-way stretched film of near balanced orientation, the total trans content increases in value, this change reflecting the increase in the crystalline trans content (Table VIII). In contrast to the one-way stretched, highly strained structures, the molecular axial order  $\Delta_{\sigma}$  of these films remains essentially unchanged while the amount of molecular uniplanar structure,  $\Delta_p$  increases (Table VIII). It is felt that the greater mobility of the biaxially stretched structure is such that the near-neighbor gauche segments, having acquired sufficient thermal energy to isomerize, easily shift into *trans* segments, which crystallize. Subsequent crystallite growth produces a volume decrease which exerts additional tensile forces on the trans segments and forces them into a uniplanar configuration, i.e.,  $\Delta_{\mathbf{p}}$  increases. During the nonrestrained crystallization of two-way stretched films, the amorphous trans content decreases appreciably, the crystalline trans content increases, and  $\Delta_p$  de-The amorphous regions are relaxed. creases.

#### **Post-Stretching**

If the essentially balanced, crystallized, two-way stretched film is subsequently given an additional M.D. stretch, i.e., by post-stretching, the molecular chain segments are once again shifted toward the machine direction but are now more constrained in their motion by the additional crystallinity present (Table III). As a result, the molecular chain segments in the amorphous regions are drawn taut. Infrared measurements show that the amount of *trans* crystalline structure remains essentially unchanged, but that the amount of *trans* amorphous structure has increased



Fig. 3. Tensile  $F_5$  vs. shrinkage, long period vs. shrinkage.

(Table III). X-ray measurements show that the crystallite lengths remain essentially unchanged, but that the long-period spacings have increased (to beyond 125 A.), so that the distance between crystallites (the amorphous length) has increased (Table III). This very taut structure is difficult to deform further, since the chain segments in the amorphous regions are already extended in a variety of directions, thereby limiting the freedom that can occur during additional stretching, e.g., during tensile testing. Low elongations, high modulus, and high  $F_5$  values are, therefore, produced (Table VI).

### **Strain Relaxation**

One of the most significant features exhibited by these taut extended amorphous structures is the ability to relax easily and generate new structural and property features. For example, if a one-way stretched film is heated to a temperature of  $100^{\circ}$ C. for a short time without the application of tension, there is a large decrease in the amorphous *trans* content, little or no change in the crystalline *trans* content, along with a decrease in the



Fig. 4. Density vs. shrinkage.

amount of molecular alignment,  $\Delta_a$  and  $\Delta_p$  (Table IX). Evidence for the strained or taut amorphous structure which accounts for the high tensile properties in one-way and post-stretched films is found in the thermal relaxation results given in Tables IX and X. Figure 3 shows the degeneration of the  $F_5$  and long period as the film is thermally relaxed. If this strain relief is caused by a change in the tautness of the segments in the amorphous regions, it should be reflected in several ways. For example,



Fig. 5. M.D. elongation vs. shrinkage.

the amorphous length should become smaller and the chain segments should coil or fold into a more compact structure. As a consequence, lower longperiod values and higher elongations and density should be observed. Each of these effects does occur, as shown in Figures 4 and 5. Balanced, two-way stretched heat-set films with a less taut amorphous structure do not exhibit these effects to the same magnitude. One further structural change deserves mention, since it is indicative of the interdependence of crystallite orientation and highly strained amorphous regions. Relaxation of the strained amorphous structure causes very little change in the alignment of crystallite c axes, i.e., the change in  $\sigma_{(a,a)}$  is small, but the crystallites do rotate out the plane of the film, i.e., increasing  $\sigma_{(p,p)}$ . This again emphasizes the necessity of having independent measurements of both the crystalline and amorphous structural parameters. Apparently, the high uniplanarity of the crystalline structure produced in stretched films is at least partially due to coplanar tensile forces applied by means of the connecting segments in the amorphous region.

#### Discussion

We have attempted to present a comprehensive view of the structural changes taking place in poly(ethylene terephthalate) films resulting from stretching, crystallization and thermal relaxation using several measurement techniques. Basically the system is an initially amorphous unoriented polymer which develops strain-induced crystallinity during stretching and then undergoes a secondary crystallization upon subsequent thermal treatment. Three structural factors influence resultant film properties: (1) the kind and perfection of crystallite orientation, (2) the amount and direction of the *trans-gauche* isomerization in the amorphous regions, and (3) the amount of crystallinity. The degree of interaction of these factors results in substantially different film properties and relaxation behavior. It is not our intent here to discuss the various models of polymer morphology that have been proposed. However, we feel that our results are plausible in the context of a crystalline and amorphous system having a broad degree of order between these extremes.

Most studies of crystalline polymers have been almost exclusively concerned with crystal morphology and the amount of crystallinity. The thesis we have tried to present here is that the so-called amorphous region is an often neglected area for work, since it contributes substantially to an understanding of the structural changes that occur.

#### APPENDIX

## Method of Calculating the Crystallite Orientation Distribution Parameters $(\sigma_{a,a})$ and $\sigma_{(p,p)}$

The x-ray intensity distribution curves obtained from specific sample rotations on the single crystal orienter can be considered as a distribution of mass, with the x-ray intensity at a given angle, a measure of the number of mass elements occupying that position. The problem then is to determine the center of gravity of the curve. This was the procedure used to define the crystallite orientation distributions by a single number. The x-ray intensities at 5° intervals in the range 0-90° were measured and coded  $f_0$  to  $f_{18}$  and the distance from 0°,  $X_n = 0.5$  to 18.5. Other arithmetic scales could have been used for  $X_n$  but these were found to be convenient.  $\sigma_{(x,p)}$  and  $\sigma_{(a,a)}$  were calculated by numerical integration as follows:

$$\sigma = \sum f_n X_n / \sum f_n \tag{1}$$

where

$$\sum f_n = f_0 + f_1 + \ldots + f_{18}$$
$$\sum f_n X_n = f_0 (0.5) + f_1(1.5) + f_2(2.5) + \ldots + f_{18}(18.5)$$

It is often more convenient to discuss the curves in terms of the angle of orientation. This is done by multiplying eq. (1) by the size of the angular increment,  $5^{\circ}$ , and subtracting one-half the increment, i.e.,

$$\sigma^{\circ} = \left[ (\sum f_n X_n) / (\sum f_n) \right] (5^{\circ}) - 2.5^{\circ}$$
 (2)

Perfect orientation now equals  $0^{\circ}$  and a random distribution,  $45^{\circ}$ . Equation (2) was used for the values given in the tables.

Several minor errors influence the values of  $\sigma_{(p,p)}$  and  $\sigma_{(a,a)}$ . Among these are differences in sample density, sample volume, and the total x-ray intensity used to make the measurements. To point out the magnitude of one of these errors, that due to gross changes in the x-ray intensity, a sample was measured with an old x-ray tube (>2000 hr.) and a new one. The  $\sigma_{(p,p)}$  and  $\sigma_{(a,a)}$  values differ in the two cases by less than 1° for a difference in total intensity of greater than 2.5 times (Table XI).

	*		
Total intensity	Old tube	New tube	Change in
maximum of the	(9200	(24,500	distribution
(100) plane	counts/sec.)	counts/sec.)	index
σ(p,p)	11.73°	10.76°	$\Delta \sigma_{(p,p)} = 0.97^{\circ}$ $\Delta \sigma_{(a,a)} = 0.47^{\circ}$
σ(a,a)	39.28°	38.81°	

TABLE XI

Small differences in sample volume and density likewise introduce only small errors. Absorption differences are shown to be negligible by rotating the sample parallelepiped<sup>1</sup> through  $360^{\circ}$ , during which the diffracted intensity fluctuations are within the counting error.

The similarity between methods used by two other authors to calculate the orientation angle are given below in eqs. (3-5) with the use of similar notation:

Hermans:7

$$\langle \sin^2 \phi \rangle = \int_0^{\pi/2} \sin^2 \phi I_{(\phi)} \sin \phi d\phi \Big/ \int_0^{\pi/2} I_{(\phi)} \sin \phi d\phi$$

Wilchinsky:5

$$\langle \cos^2 \phi \rangle = \int_0^{\pi/2} \cos^2 \phi I_{(\phi)} \sin \phi d\phi \Big/ \int_0^{\pi/2} I_{(\phi)} \sin \phi d\phi$$

This work:

$$\sigma_{(p,p)} = \langle \phi \rangle = \int_0^{\pi/2} I_{(\phi)} \phi d\phi \bigg/ \int_0^{\pi/2} I_{(\phi)} d\phi$$

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#### Résumé

Une étude a été effectuée sur les changements de structure et de propriétés qui ont lieu lorsque des films de téréphtalate de polyéthylène sont orientés, cristallisés et détendus thermiquement. Des mesures de diffraction aux rayons X, à l'infrarouge, de densité et de tension-élongation ont été employées pour obtenir des informations concernant la quantité et la direction d'orientation des régions cristalline et amorphe de ces films. Trois facteurs de structure influencent les propriétés finales du film: (1) la sorte et la perfection de l'orientation cristalline, (2) la quantité et la direction de l'isomérisation trans-gauche dans les régions amorphes et (3) la quantité de cristallinité . Les interactions de ces facteurs proviennent des propriétés pratiquement différentes du film et du comportement à la relaxation. Une importance spéciale est à attribuer à l'influence des régions amorphes étendues produites par une orientation qui procure une information utile sur la relation structure-propriété.

#### Zusammenfassung

Eine Untersuchung der Struktur- und Eigenschaftänderungen, welche während der Orientierung, Kristallisation und thermischen Relaxation von Polyäthylenterephthalatfilmen auftreten, wurde durchgeführt. Röntgenbeugungs-, Infrarot-, Dichte- und Spannungs-Dehnunsmessungen wurden verwendet, um eine Information über den Betrag und die Richtung der Orientierung in den kristallinen und den amorphen Bereichen dieser Filme zu erhalten. Drei Strukturfaktoren beeinflussen die resultierenden Filmeigenschaften: (1) Art und Vollkommenheit der Kristallitorientierung, (2) Betrag und Richtung der trans-gauche-Isomerisierung in den amorphen Bereichen und (3) der Betrag an Kristallinität. Wechselwirkungen zwischen diesen Faktoren führen zu wesentlich verschiedenen Filmeigenschaften und unterschiedlichem Relaxationsverhalten. Besonders bemerkenswert ist der Einfluss von "straff" gespannten, durch Orientierung erzeugten amorphen Bereichen, welche brauchbare Struktur- und Eigenschaftsinformationen liefern.

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